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For all transportablo goods industries as a whole, O Herlihy has studied both short run and long run responses of employment to the output level [3]. His findings with regard to long term changes are that employment tends to rise by about $6 \%$ for every $10 \%$ increase in incustrial output; minus a $1.2 \%$ reduction per annum which reflects autonomous labour productivity gains.


#### Abstract

It is of some interest to ascertain whethor similar relationships to that developed on a global level apply to individual industry groups. For this purpose, recently published annual index numbers of production and data for persons engaged in industry [1] each year for 1953 to 1964 have now been analysed.

The data were converted into firet differences of logarithms, and initially separate employment functions were estimatod for each industry group. All equations were of the form


$$
\Delta \log _{e} L=a+b_{1}\left\{\log _{e} P+b_{2} \log _{e} P_{-1}\right.
$$

where $L$ indicates employment and $P$ output. Thus the more immediate and the further delayed effects of output changes on employment changes were separately estimated; a finer lag structure could of course not be ascertained with annual data. It seemed reasonable to assume that any adjustment to changes in production levels would be completed a year later on. The results were as follows, using the ycar-to-year changes from 1954-5 to 1964-5, and 1953-4 for the lagged variable.

Table 1. Coefficients in employment functions for each industry group, $1954-5$ to 1963-4

| Industry group | a | ${ }^{\circ} 1$ | $\mathrm{b}_{2}$ | $x^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
|  | (constant) | $\left(i, \log _{0} \mathrm{~F}\right)$ | $\left(L_{0} \mathrm{log}_{0} \mathrm{P}_{-1}\right.$ ) |  |
| Food | -. 00042 | $\begin{aligned} & .4154 \\ & (.1388) \end{aligned}$ | $\begin{gathered} .1053 \\ (.0983) \end{gathered}$ | . $70 \%$ |
| Drink and tobacco | $-.00518$ | $\begin{aligned} & .2971 \\ & (.1632) \end{aligned}$ | $\begin{gathered} .1069 \\ (.1642) \end{gathered}$ | . 406 |
| Textiles | -. 01592 | $\begin{gathered} .4993 \\ (.1422) \end{gathered}$ | $\begin{gathered} .0726 \\ (.1 .243) \end{gathered}$ | . 665 |
| Clothing and footwear | -. 01183 | $\begin{aligned} & .3798 \\ & (.0632) \end{aligned}$ | $\begin{aligned} & .0104 \\ & (.0617) \end{aligned}$ | . 058 |
| Wood and furniture | $-.02631$ | $\begin{aligned} & .5634 \\ & (.1490) \end{aligned}$ | $\begin{aligned} & .0869 \\ & (.1470) \end{aligned}$ | .767 |
| Paper and printing | -. 01383 | $\begin{aligned} & .1769 \\ & (.1444) \end{aligned}$ | $\begin{gathered} .3752 \\ (.1239) \end{gathered}$ | . 672 |
| Chemicals | -. 01348 | $\begin{aligned} & .3798 \\ & (.1 \angle 00) \end{aligned}$ | $\begin{aligned} & .2333 \\ & (.1404) \end{aligned}$ | . 557 |
| Structural clay and cement | -.02304 | $\begin{aligned} & .4625 \\ & (.0797) \end{aligned}$ | $\begin{gathered} .2533 \\ (.0826) \end{gathered}$ | . 395 |
| Netals and enginooring | -. 00950 | $\begin{gathered} .4920 \\ (.0941) \end{gathered}$ | $\begin{gathered} .1810 \\ (.0825) \end{gathered}$ | . 362 |
| Other manufacturing | -. 00596 | $\begin{aligned} & .3786 \\ & (.0904) \end{aligned}$ | $\begin{aligned} & .0904 \\ & (.0917) \end{aligned}$ | . 771 |
| Mining and turf | . 00156 | $\begin{gathered} .1352 \\ (.1022) \end{gathered}$ | $\begin{gathered} .0993 \\ (.1017) \end{gathered}$ | .201 |

It is immediately evident that the relationship for mining and turf is quite different in character from those for the manufacturing industry groups; there is a small autonomous loss in labour productivity instead of a gain, changes in output have only a slight effect upon employment and explain only one-fifth of the variation in relativo employment changes instead of anything between $40 \%$ and $90 \%$. Variations in the supply of turf which are not planned but brought about by climatic conditions are probably largely responsible for this state of affairs. For this reason, mining and turf has been excluded from further analysis, which thus refers to manufacturing industries above.

One would expect current changes in output to havo a greater effect upon employment than changes in the past year; and this in fact appears to be borne out by the results for all but one industry group. Howevor, with only 7 degrees of freedom available for each group, the regression coefficients cannot bo accurately estimated. More reliable results can be obtained if pooling of the observation is permissible.

An analysis of variance which was carried out shows that the regression coefficient for the 10 industry groups do indeed not differ significantly, the relevant F ratio being only . 70. Regarding the differences between constant terms, we find that $F=1.74$, which is just significant at the $10 \%$ level. Thus a single equation may be considered, but a set of parallel equations scems theoretically quite plausible and may well be given preference. The results obtained follow.

$$
\Delta \log _{\mathrm{e}} \mathrm{~L}=-.01351+\underset{(.0343}{(.0324)} \begin{array}{r}
.0 \log _{\mathrm{e}} P+.1544 \\
(.0308)
\end{array} \log _{\mathrm{e}} \mathrm{P}_{-1}
$$

or:

$$
\angle \log _{e} L=a+\underset{(.0325)}{.0396} \log _{e} P+(.1614) \Delta \log _{e} P_{-1}
$$

Where a assumes the following values:

| Food | -.00166 |
| :--- | ---: |
| Drink and tobacco | -.00632 |
| Textiles | -.01771 |
| Clothing and footwear | -.01853 |
| Wood and furniture | -.02532 |
| Paper and printing | -.01964 |
| Chemicals | -.01251 |
| Structural clay and cement | -.01571 |
| Metals and engineering | -.00445 |
| Other manufacturing | -.01850 |
| $\quad$ Mean | -.01414 |

$$
\text { For the single equation, } \mathbb{R}^{2}=.769 . \quad \text { For }
$$

$$
\text { the parallel equations, } R^{2}=.764, \text { or } X^{2}=.304 \text { if }
$$

calculated on the basis of deviations from industry group means.

Thus the analysis confirms the carlier result that a $10 \%$ change in industrial output tends to be accompauicd by a $6 \%$ change in employment in the same direction, about three-quarters of the adjustment taking place in the current and one-ouartor in tho following year. The gains in labour productivity which are not associated with incustrial growth appoar to lie within the range of $1-2 \%$ per annum for most industry groups, though less for food, for drink and tobacco, and for metals and engineering, but more for wood and furniture.

As a check on the validity of tho employment function, a further regression has been computed, using cross section data for 41 individual industries for which data referring to 1953 and 1964 are available. Denoting here by $P$ the volume of production in $196 \Omega$ divided by 100 and by $L$ the employment in 1964 divided by employment in 1953, the resulting equation is

$$
\log _{e} L=\frac{-.0703}{(.0661)}+\left(.0765 \log _{e} P \quad\left(R^{2}=. .641\right)\right.
$$

Thus, the long-run elaoticity of employment with regard to output is again estimated to be in the neigh bourhood of 0.6 . Since the constant term reflects the total trend effect of the 11 year period, the average annual autonomous gain in labour productivity is now estimated to be about $0.6 \%$ or $0.7 \%$ instead of 1. 4 . However, the trend is not accurately estimated by this method which compares industries of very diverse oizo and oxporionco. The employment functions derived for industry groups should be the more reliable and useful ones.

The equations may be used to check the N.I.E.C. industrial employment forecasts for 1970 [2]. On the Dasis of the estimated volume of output changes between 1964 and 1970 and those between 1963 and 1969 , using 1969 figures obtained by geometric interpolation between 1967 and 1970, employment changes may be estimated and converted into actual numbers in 1970. The results are as follows:
Table 2. Estimated employment in manufacturing
industry groups, 1970

| Industry group | Employment (000) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 1964 | 1970 |  |  |
|  |  | Single equation | farallel <br> equations | $\begin{aligned} & \text { N.J.D.S. } \\ & \text { estimato } \end{aligned}$ |
| Food | 38.8 | 42.5 | 45.9 | 43.9 |
| Drink and tobacco | 10.2 | 10.3 | 10.8 | 10.7 |
| Textiles | 22.3 | 24.9 | 24.4 | 23.2 |
| Clothing and footwoar | 22.7 | 23.3 | 22.7 | 23.5 |
| Wood and furniture | 7.3 | 9.5 | 8.9 | 9.6 |
| Paper and printing | 14.3 | 15.4 | 14.3 | 16.0 |
| Chemicals | 5.9 | 3.2 | 3.3 | 7.9 |
| Structural clay and cement | 7.2 | 3.3 | 8.0 | 2.8 |
| Metals and engineering | 31.9 | 39.0 | 41.4 | 40.1 |
| Cther manufacturing | 10.2 | 13.0 | 12.4 | 14.3 |
| A11 manufacturing | 171.8 | 194.9 | 198.4 | 198.0 |

Thus according to whether the trend effect is assumed to be the same for all industry groups or to vary between industries, total manufacturing employment is expocted to increase by about $13 \frac{1}{2} \%$ or by about $15 \frac{1}{2} \%$ between 1964 and 1970. The forecast on the basis of variable autonomous labour productivity increases practically coincides with the $N . I . B . C$. estimate as far as total manufacturing employment is concerned, though there are discrepancios for individual industry groups, notably food, textiles, paper and printing, metals and engineering, and all manufacturing.

Time will show which of the estimates proves more accurate. Of course, the accuracy of all forecasts depends on to what extent output targets will be reached.

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